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THEORY OF THE CURRENT-DRIVEN ION CYCLOTRON INSTABILITY  
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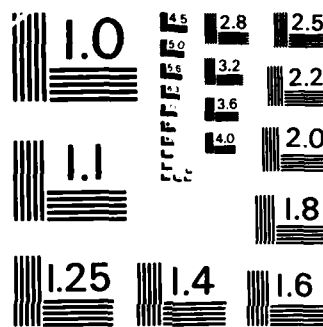
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# Theory of the Current-Driven Ion Cyclotron Instability in the Bottomside Ionosphere

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November 11, 1985

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19 ABSTRACT (Continue on reverse if necessary and identify by block number) <p>A theory of the current-driven electrostatic ion cyclotron (EIC) instability in the collisional bottomside ionosphere is presented. It is found that the electron collisions are destabilizing and are crucial for the excitation of the EIC instability in the collisional bottomside ionosphere. Furthermore, the growth rates of the ion cyclotron instability in the bottomside ionosphere maximize for <math>k_{\perp} \rho_i \gg 1</math> where <math>2\pi/k_{\perp}</math> is the mode scale size perpendicular to the magnetic field and <math>\rho_i</math> the ion gyroradius. Realistic plasma density and temperature profiles typical of the high latitude ionosphere are used to compute the altitude dependence of the linear growth rate of the maximally growing modes and critical drift velocity of the EIC instability. The maximally growing modes correspond to observed meter size irregularities and the threshold drift velocity required for the excitation of EIC instability is lower for heavier (<math>\text{NO}^+</math>, <math>\text{O}^+</math>) ions than that for the lighter (<math>\text{H}^+</math>) ions. Dupree's resonance broadening theory is used to estimate nonlinear saturated amplitudes for the ion cyclotron instability in the high latitude ionosphere. Comparison with</p>										
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## 19. ABSTRACT (Continued)

experimental observations is also made. It is conjectured that the EIC instability in the bottomside ionosphere could be a source of transversely accelerated heavier ions and energetic heavy ion conic distributions at higher altitudes.

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# THEORY OF THE CURRENT-DRIVEN ION CYCLOTRON INSTABILITY IN THE BOTTOMSIDE IONOSPHERE

## 1. Introduction

Electrostatic ion cyclotron (EIC) waves are one of the more important plasma wave modes in the near earth space plasma environment. Recently, EIC waves have been invoked to explain, among other effects, strong perpendicular ion heating leading to the formation of ion conics [Okuda and Ashour-Abdalla, 1981]. Ion cyclotron wave phenomena have been observed both at high (several  $R_E$ ) and low ( $< 1000$  km) altitudes along auroral field lines. Kintner et al. [1978, 1979] have reported  $H^+$  EIC wave observations using S3-3 satellite data at high altitudes in the auroral zone. At low altitudes,  $O^+$  EIC waves have been observed [Ogawa et al., 1981] on a sounding rocket equatorward of a discrete auroral arc. Yau et al. [1983], also using sounding rocket data, have reported particle and wave observations of low altitude (400-600 km) ionospheric ion acceleration events consistent with ion cyclotron wave phenomena. Bering [1984] has given indirect, but compelling, evidence of short wavelength ( $k_{\perp} \rho_i \geq 1$  where  $2\pi/k_{\perp}$  is the density fluctuation scale size perpendicular to the magnetic field and  $\rho_i$  is the ion gyroradius) ion cyclotron wave activity at low altitudes ( $< 350$  km) in the diffuse aurora using sounding rocket data. Evidence for short wavelength ( $k_{\perp} \rho_i \geq 1$ ) ion cyclotron wave emissions in the auroral E-region has been presented by Fejer et al. [1984] using backscatter radar observations. Photometric observations in the bright auroras at  $\sim 130$  km altitude by Martelli et al. (1971) indicated excitation of EIC waves at frequencies lying between 25 and 32 Hz, corresponding to gyrofrequencies of  $NO^+$  and  $O_2^+$ . Bythrow et al. (1984), using Hilat satellite data, have concluded that the very large earthward directed currents seen near the equatorward edge of the diffuse aurora exceed the threshold for the excitation of ion cyclotron waves.

Kindel and Kennel [1971] first discussed the ion cyclotron instability in a space plasma context by showing that the electrostatic ion cyclotron instability has the lowest threshold among various current-driven instabilities in the high latitude auroral space plasma. They only briefly discussed the role of weak collisional effects on the evolution of the EIC wave instability. They did note, however, in the context of the EIC

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instability that electron collisions were destabilizing and ion collisions were stabilizing. Physically, the ion cyclotron instability is related to the dissipative effect on electrons in their parallel motion which impedes the "instantaneous" redistribution of the electron fluid to a Boltzman-like distribution in the wave potential. In the collisionless limit, the dissipation is due to the wave-particle (Landau) resonance, while in the collisional case, it is caused by the electron collisions with ions (or neutrals). The results of Kindel and Kennel [1971] are only applicable to the collisionless and weakly-collisional topside ionosphere [Chaturvedi et al., 1984]. Recently Ganguli et al. (1985) have proposed a mechanism that depends on the inhomogeneity of the transverse electric fields to generate ion cyclotron waves in a collisionless plasma in the absence of field-aligned currents. However, several of the aforementioned experimental studies have indicated ion cyclotron wave emissions can occur at low altitudes in the collisional bottomside ionosphere. D'Angelo [1973], using the work of Varma and Bhadra [1964] and Levine and Kuckes [1966], has shown that the current-driven EIC instability might be excited at low altitudes (E-region) where the ion-neutral collision frequency is comparable to the ion cyclotron frequency. This work has been extended to the collisional auroral F-region altitudes by Chaturvedi [1976] based on the analyses of Chaturvedi and Kaw [1975] and Milic [1972]. However, Chaturvedi [1976] considers collisional effects on the ion cyclotron instability using a fluid approximation ( $k_{\perp} \rho_i < 1$ ). This analysis is not applicable to the recent experimental observations which indicate  $k_{\perp} \rho_i \geq 1$ . For example, Bering (1984) and Fejer et al. (1984) have reported observations of meter size irregularities corresponding to  $k_{\perp} \rho_i \approx 1$ . Indeed, the transition between collisionless and collisional excitation of the ion cyclotron instability, the approximate altitude of this transition, and the dependence of growth rate of the ion cyclotron instability on ambient high latitude ionospheric plasma parameters is not well-defined.

In addition to observations indicating existence of EIC waves in the bottomside ionosphere, the presence of energetic heavy ions at 1400 km altitude was first documented by Hoffman et al. [1974]. Energy and pitch angle distributions of various ion species obtained by S3-3 and PROGNOZ-7 satellite measurements provide evidence for the presence of energetic heavier ion species ( $\text{NO}^+$  and  $\text{O}^+$ , for example) at altitudes of a few



thousand kilometers or more (Hultqvist, 1983; Yau et al., 1984). The pitch angle distributions of ions ranged from being field-aligned (ion beams) to conical, in which case the flux peaks at an angle to the geomagnetic field. The pitch angle distributions measured at energies less than 650 eV are relatively field-aligned, while those at 1 keV and above have a conical distribution with no field-aligned component [Klumpar et al., 1984]. Recent data from DE-1 also showed that the high altitude Polar Cap region contains upflowing heavy molecular ions such as  $\text{NO}^+$ ,  $\text{O}_2^+$  and  $\text{N}_2^+$  (Craven et al., 1985). These data suggest that the source for these energetic heavy ions might be located in the ionosphere (Hultqvist, 1983). Based on our linear theoretical analysis, we conjecture that the current driven EIC waves at the ion (heavy) cyclotron frequency could selectively accelerate the heavier ions, such as  $\text{NO}^+$ ,  $\text{O}_2^+$  and  $\text{O}^+$ , in the transverse direction. Thus the bottomside ionosphere can act as a source for the heavier ion conics observed at magnetospheric altitudes.

In this paper we study the EIC instability in the bottomside collisional ionosphere. We find that the growth rates of the EIC instability in the bottomside ionosphere maximize for  $k_{\perp} \rho_i = 1$ . In Sec. 2, we present the general dispersion relation for EIC waves in a collisional plasma which we solve analytically both in the collisionless, weakly collisional, and strongly collisional limits. We also solve the full dispersion relation numerically, using the plasma density and temperature profiles obtained from the Sondrestrom radar (Kelly, 1983). The dispersion relation is solved for the maximally growing modes, for which  $k_{\perp} \rho_i = 1.4$ , corresponding to observed meter size irregularities. In Sec. 3, we compute expected nonlinear saturation amplitudes of the electrostatic ion cyclotron instability in a collisional plasma based upon Dupree's resonance broadening theory and compare with experimental observations. Finally in Sec. 4, we summarize and discuss our results.

## 2. Linear Theory

We consider a homogeneous plasma in a uniform magnetic field along the  $z$ -direction,  $\underline{B} = B \hat{z}$ . The plasma is collisional and the main source of free energy is due to the magnetic field aligned currents. In this paper we ignore inhomogeneous effects, e.g., density and temperature gradients and, as a result, use local theory. Furthermore, we assume the scale height in

the high latitude ionosphere to be much larger than the parallel wavelengths involved. In our attempt to understand ion cyclotron instabilities in the bottomside ionosphere, we include collisional effects and use the general dispersion relation derived by Clemmow and Dougherty (1969). In order to include collisional effects we use a number conserving BGK collision model. This model can also be shown to conserve momentum if the electrons are assumed to carry the bulk of the current and the ions are considered to be at rest. Under these conditions, the BGK model reproduces well electron-neutral ( $\nu_{en}$ ), electron-ion ( $\nu_{ei}$ ), and ion-neutral ( $\nu_{in}$ ) collisions. However, the BGK model does not reproduce well ion-ion ( $\nu_{ii}$ ) or electron-electron collisions and a different collision model, e.g., Fokker-Planck approximation, must be used. Since we will be considering bottomside F-region altitudes ( $z \leq 300-400$  km),  $\nu_{ii} \leq \nu_{in}$  is satisfied. Electron viscous effects ( $\nu_{ee}$ ) are negligible because the electron Larmor radius is much smaller than the perpendicular wavelengths of interest. In section 2.2, we do include a phenomenological model for  $\nu_{ii}$  in our numerical computation of growth rates and marginal stability criteria for the electrostatic ion cyclotron instability.

We utilize the dispersion relation derived by Clemmow and Dougherty (1969). We list only the salient features of the derivation here. The equilibrium function is a drifting Maxwellian

$$f_{0j} = N_{0j} \left( \frac{m_j}{2\pi T_j} \right)^{3/2} \exp[-(v_{\perp}^2 + (v_{\parallel} - v_{dj})^2)/V_j^2] \quad (1)$$

where  $N_{0j}$ ,  $m_j$ ,  $T_j$ ,  $v_{dj}$  and  $V_j$  are the density, mass, temperature, drift and thermal velocities of the  $j^{\text{th}}$  species, respectively. The perturbed distribution function (where  $f_j = f_{0j} + f_{1j}$ ) is given as, using a BGK collision model,

$$\frac{\partial f_1}{\partial t} + \underline{v} \cdot \frac{\partial f_1}{\partial \underline{x}} + \frac{e}{mc} (\underline{v} \times \underline{B}) \cdot \frac{\partial f_1}{\partial \underline{v}} = \sum_j \nu_j [f_{1j} - (N_{1j}/N_{0j}) f_{0j}] \quad (2)$$

where

$$N_{1j} = \frac{-(e/m) \nabla \phi_1 \int D^{-1} \partial f_0 / \partial v \, d^3v}{1 - (\nu_j/N_0) \int D^{-1} f_0 \, d^3v} \quad \text{and } D \equiv i(\omega - i\nu_j - \underline{k} \cdot \underline{v})$$

For a low  $\beta$  ( $8\pi nkT/B^2 \ll 1$ ) plasma and perturbations of the form  $f_1 \propto \exp[-i(\omega t - \underline{k} \cdot \underline{x})]$  the dispersion relation is given as [Kindel and Kennel, 1971]

$$-k_{\perp}^2 = \sum_j \frac{\sum_n \left( \frac{\Gamma_n(b_j)}{\lambda_{dj}^2} \right) \left[ 1 + \frac{\tilde{\omega}_j}{k_{\parallel} v_j} Z(\xi_j) \right]}{1 + \left( \frac{iv_j}{k_{\parallel} v_j} \right) \sum_n \Gamma_n(b_j) Z(\xi_j)} \quad (3)$$

where

$$b_j = k_{\perp}^2 \rho_j^2 / 2$$

$$\rho_j = v_j / \Omega_j$$

$$\Omega_j = q_j B / m_j c$$

$$\lambda_{dj} = (T_j / 4\pi n_j q_j^2)^{1/2}$$

$$v_j = 2T_j / m_j$$

$$\tilde{\omega}_j = \omega - k_{\parallel} v_{dj} + iv_j$$

$$\xi_j = \frac{\tilde{\omega} + n\Omega_j}{k_{\parallel} v_j}$$

$$\Gamma_n = I_n(b_j) e^{-b_j}$$

where  $I_n(b)$  is the modified Bessel function of  $n^{\text{th}}$  order and  $Z(\xi)$  is the plasma dispersion function, and  $v_j = v_{jn}$  is the collision frequency of the  $j^{\text{th}}$  species with neutrals and  $q_j$  is the charge of the species ( $\pm e$ ). In the case of electrons, Coulomb collisions can also be included and we define  $v_e = v_{ei} + v_{en}$ .

The effects of collisions are reflected in the shifted frequency  $\bar{\omega}$  (by  $iv_j$ ) and more importantly in the additional term proportional to  $v_j/k V_j$  in the denominator of Eq. (3). In fact, this term gives rise to instability in the collisional domain. This local dispersion relation is assumed to describe both the collisional bottomside and collisionless topside ionosphere. We assume quasi-neutrality and solve equation (3) analytically in the collisionless, weakly collisional, and strongly collisional (fluid) limits.

## 2.1 Collisionless Domain

By setting  $v_j = 0$  in equation (3) we immediately recover the collisionless dispersion relation (Drummond and Rosenbluth, 1962; Kindel and Kennel, 1971). Furthermore if we set  $n = 0$  for electrons and  $n = 1$  for ions and expand the plasma dispersion function  $Z(\xi)$  such that the electrons are treated kinetically and the ions are treated in the fluid limit ( $\xi_e \ll 1$  and  $\xi_i \gg 1$ , respectively) we obtain their results:

$$\omega_r/\Omega_i = 1 + \tau \Gamma_1(b_i) \quad (4)$$

$$\gamma/\Omega_i = -\tau (\pi/2)^{1/2} \Gamma_1(b_i) \frac{(\omega_r - k V_d)}{k V_e} \quad (5)$$

where  $\tau = T_e/T_i$  and  $V_d = V_{de} - V_{di}$ . We note here that, as will be shown in sec. 2.2, the numerical solutions of equation (3) agrees with equations (4) and (5) if  $n = 1$  for ions. However, for  $n > 1$  a higher growth rate is observed, which saturates for  $n = 4$ . Consequently, the critical drift velocities given in Kindel and Kennel (1971) are overestimated and the growth rates are underestimated.

## 2.2 Weakly Collisional Limit

The analysis in this limit was also attempted by Kindel and Kennel (1971). We expand the electron Z-function in the small argument limit,  $\xi_e \ll 1$ , and retain only  $n = 0$  terms in the electron part of the dispersion relation. The electron contribution to equation (3) is given as

$$D_e = \frac{1}{\tau} \frac{1 + i \sqrt{\pi} \xi_e}{1 - \sqrt{\pi} \frac{v_e}{k v_e} \xi_e}$$

$$= \frac{1}{\tau} \left[ 1 + i \sqrt{\pi} \frac{(\omega - k v_d)}{k v_e (1 - \sqrt{\pi} v_e / k v_e)} \right] \quad (6)$$

Here we have assumed  $b_e \ll 1$  which gives  $\Gamma_0(b_e) \approx 1$ . We expand the ion Z-function in the large argument limit,  $\xi_i \gg 1$ . The ion contribution of equation (3) is given as

$$D_i = - \frac{\sum_n \frac{\omega + i v_i}{\omega + n\Omega + i v_i} \Gamma_n(b_i)}{1 - i v_i \sum_n \frac{\Gamma_n(b_i)}{\omega + n\Omega + i v_i}} \quad (7)$$

For  $v_i/\Omega_i < 1$  the ion contribution becomes

$$D_i = - f_n [(\omega - v_i^2 f_n) + i v_i (1 + \omega f_n)] \quad (8)$$

where

$$f_n \equiv \sum \frac{\Gamma_n}{\omega + n\Omega + i v_i}. \quad (9)$$

For  $v_i/\omega < 1$  the dispersion relation then becomes  $D = D_e + D_i = 0$  or

$$\frac{1}{\tau} \left[ 1 + i \pi \Gamma \frac{(\omega - k v_d)}{k v_e (1 - \Gamma_1 v_e / k v_e)} \right] = - f_n (\omega + i v_i + \omega v_i f_n) \quad (10)$$

From the real part of equation, we obtain the usual result

$$\omega_r = \Omega_i [1 + \tau \Gamma_1(b_i)] \quad (11)$$

and from the imaginary part we obtain

$$\gamma/\omega_r = - 2 \sqrt{\pi} \tau \Gamma_1(b_i) \frac{(\omega_r - k v_d)}{k v_e} \left( 1 + \sqrt{\pi} \frac{v_e}{k v_e} \right) - v_i/\Omega_i \left( 1 + \frac{1}{\tau} \right) \quad (12)$$

which leads to the collisionless result of Drummond and Rosenbluth (1962) and Kindel and Kennel (1971) in equation (5) when  $v_e = v_i = 0$ . Equation (12) shows that the electron collisions have a destabilizing influence whereas the ion collisions are stabilizing. In the short wavelength limit,  $v_e/k v_e \ll 1$ , the ion collisions override the destabilizing influence of electron collisions. However, we show in the next section that the electron collisions dominate the ion collisions in the fluid limit,  $v_e/k v_e \gg 1$ .

### 2.3 Strongly collisional limit

In this limit the electron mean freepath  $\lambda_e \ll \lambda_i$  and thus  $v_e/k v_e \gg 1$ . For  $v_e/k v_e \gg 1$ , we can expand the electron Z-function in the large argument limit while still satisfying  $v_i < v_d \leq v_e$ , obtaining

$$D_e = -\frac{1}{2\tau} \frac{\Gamma_0(b_e)}{\xi_e^2 - \frac{i v_e}{k^2 v_e^2} \tilde{\omega} (1 + 1/2 \xi_e^2) \Gamma_0(b_e)} \quad (13)$$

The ion contribution is obtained, as before, by expanding the Z-function in the large argument limit,  $\xi_i \gg 1$ , as

$$D_i = G - \Gamma_1(b_i) \frac{\omega}{\omega - \Omega_i} \quad (14)$$

where

$$G = 1 - \frac{1 - \Gamma_0(b_i)}{b_i} \quad (15)$$

Now, the dispersion relation becomes

$$D = D_e + D_i \approx 0$$

from which the growth rate and real frequency can be written as

$$\omega_r/\Omega_i = 1 + \tau \Gamma_1(b_i) (1 - \tau G) \left( 1 - \frac{(\Omega_i - k v_d)^2}{k^2 v_e^2} \frac{1}{\Gamma_0(b_e) + \alpha} \right) \quad (16)$$

$$\gamma/\omega_r = \frac{-2\tau\Gamma_1(b_i)(1-\tau G)}{(\Gamma_0(b_e) + \alpha)} \frac{(\omega_r - k_{\perp} V_d)v_e}{k_{\perp}^2 v_e^2} \quad (17)$$

where  $\alpha = (v_e^2/\Omega_e^2)(k_{\perp}^2/k_y^2)$ . For  $b_i \ll 1$  and  $v_e/\Omega_e \ll 1$  equations (16) and (17) reduce to that obtained by Chaturvedi (1976) who used a fluid analysis. We see from equations (16) and (17) that the real frequency is not significantly different from the collisionless result (see equation 4) and the growth rate is directly proportional to  $v_e$  and  $V_d$  but has a peak in  $v_e$  at  $v_e = \Omega_e(k_{\perp}/k_y)[\Gamma_0(b_e)]^{1/2}$ . Since  $v_e \propto T_e^{-3/2}$  for Coulomb collisions we see from equation (17) that initially the growth rate decreases with  $T_e$  as  $T_e^{-3/2}$  and for strong collisions the growth rate increases as  $T_e^{3/2}$  indicating a minimum as a function of  $\tau$  (for a fixed  $T_i$ ). This is in sharp contrast to the collisionless case where the growth rate increases as a function of  $\tau$  (equation 5).

#### 2.4 Marginal stability analysis

In the collisionless domain several authors have estimated the drift velocity thresholds for the onset of the ion cyclotron instability (see for example, Drummond and Rosenbluth, 1962; Kindel and Kennel, 1971). Kindel and Kennel (1971) have examined briefly the effects of ion-neutral collisions and weak electron-neutral collisions. Their expression for threshold drift velocity shows that while the electron-neutral collisions could destabilize the EIC instability, the ion-neutral collisions strongly stabilize the EIC instability.

In the weakly collisional limit  $v_e/k_{\perp} v_e \ll 1$ , we expand the electron Z-function in the small argument limit. The electron part of the dispersion relation in the above limit together with the ion part in the large argument limit yield the dispersion relation given in equation (10). The imaginary part of equation (10) yields, for  $\gamma = 0$ ,

$$\omega_r - k_{\perp} V_c = \frac{\tau}{\sqrt{\pi}} (k_{\perp} v_e - \sqrt{\pi} v_e) \frac{f_n v_i (1 + \omega_r f_n)}{(1 - v_i^2 f_n^2)} \quad (18)$$

Where  $V_c$  is the threshold drift velocity. Considering the resonance at the first harmonic we obtain from equation (18)

$$\frac{v_c}{v_e} = \frac{\omega_r}{k v_e} + \frac{\tau \Gamma_1}{\sqrt{\pi}} \left( 1 - \frac{v_e \sqrt{\pi}}{k v_e} \right) \left( \frac{v_i}{\omega - \Omega} \right) \left( 1 + \frac{\omega_r \Gamma_1}{\omega - \Omega} \right) \quad (19)$$

which agrees with that of Kindel and Kennel (1971). Equation (19) shows that in a weakly collisional limit the critical drift velocity is reduced by electron collisions and increased by ion collisions. For a given ion temperature, increasing the electron temperature increases the critical drift velocity; however, electron collisions reduce the influence of ion collisions.

In the strongly collisional limit  $v_e/k v_e \gg 1$  and  $v_e \geq \omega$ , the large argument expansion of the electron and ion Z-functions yields the dispersion relation, equation (15), from which

$$\frac{\Gamma_0(b_e) + \alpha}{[\Gamma_0(b_e) + \alpha] - 2(\bar{\omega}_e)(\omega - k v_c)/k v_e^2} + \tau \left\{ 1 + \bar{\Gamma}_1 \left[ -\frac{\bar{\omega}}{\bar{\omega} - \Omega_i} + i\sqrt{\pi} \frac{\bar{\omega}}{k v_i} e^{-\xi_1^2} \right] \right\} = 0 \quad (20)$$

where  $\bar{\Gamma}_1 = \Gamma_1(b_i) (1 + \tau G)$  and  $\bar{\omega} = \omega + i v_{in}$ . From the imaginary part of (20), we obtain for  $(\omega - k v_c)/k v_e \ll 1$

$$\frac{v_c}{v_e} = \frac{\omega_r}{k v_e} + \tau \bar{\Gamma}_1 \frac{k v_e}{v_e} \left[ \frac{v_i \Omega_i}{(\omega_r - \Omega_i)^2 + v_i^2} + \sqrt{\pi} \frac{\omega_r}{k v_i} e^{-|\xi_1|^2} \right] \quad (21)$$

where  $\omega_r$  is obtained from the real part as

$$\omega_r = \Omega_i [1 + \tau \bar{\Gamma}_1 / (1 + \tau)] \quad (22)$$

Equation (21) shows that in the strongly collisional limit the critical drift velocity has a markedly different behaviour than in the weakly collisional or collisionless limit. Even for  $v_i = 0$  the electron collisions reduce the critical drift velocity, which is not the case in the weakly collisional limit (equation 19). Furthermore, ion collisions affect the collisional result differently depending on how strong the collision frequency is compared to  $(\omega_r - \Omega_i)$ , as can be seen from the second term on the right hand side of equation (21). More importantly, the critical drift velocity has a different behaviour as a function of  $\tau$ , showing a



minimum in some domains, compared to the collisionless case, where it was shown to increase linearly with  $\tau$  (Drummond and Rosenbluth, 1962).

## 2.5 Numerical Results Applied to Auroral F-region

The dispersion relation given in equation (3) describes the obliquely propagating ion cyclotron instability and ion acoustic instability as well ( $k_{\perp} = 0, \tau > 1$ ). In this paper, we confine ourselves to the analysis of the ion cyclotron instability. We illustrate the properties of the EIC instability by solving the dispersion relation numerically using parameters typical of the high latitude ionosphere and compare the numerical results with the analytical results in various regimes of collisionality where possible. We find that the growth rate of the collisional ion cyclotron instability maximizes at  $k_{\perp} \rho_i \approx 1$ . Furthermore,  $k_{\perp} \rho_i \approx 1$  also corresponds to modes with  $\lambda_{\perp} \approx 11m$  ( $\rho_i \approx 2.56m$  for  $O^+$ ), which is on the order of typically observed scale size [Fejer et al., 1984; Bering, 1984].

Typical bottomside auroral zone ionospheric electron density and temperature profiles based on Sondrestrom incoherent scatter radar data (Kelly, 1983; C.L. Rino, private communication) are shown in Fig. 1 and 2 respectively. Curve B is taken from Kelly (1983) the data being simply extrapolated to 600 km. The two electron density profiles (A and C) are expected to bracket both quiet and disturbed conditions with corresponding F-peak densities of roughly  $10^4$  and  $10^6 \text{ cm}^{-3}$ , respectively. The electron-neutral ( $\nu_{en}$ ), electron-ion ( $\nu_{ei}$ ), ion-ion ( $\nu_{ii}$ ) and ion neutral ( $\nu_{in}$ ) collisions based upon the data in Fig. 1 and 2 are calculated using standard expressions (Spitzer, 1962; Banks and Kockarts, 1973). Fig. 3 gives the total electron collision frequency ( $\nu_e = \nu_{en} + \nu_{ei}$ ), while Fig. 4 displays the ion collision ( $\nu_i = \nu_{in} + \nu_{ii}$ ) frequency. These collision frequencies are calculated using the electron density profiles of Fig. 1 (Curve 2, Kelly, 1983). Neutral particle density profiles are taken from Banks and Kockarts, (1973) and fall off exponentially with altitude.

In order to illustrate the destabilizing effects of electron neutral and electron ion collisions on the ion cyclotron instability, we solve the dispersion relation Eq. (3) numerically varying  $\nu_e = \nu_{en} + \nu_{ei}$  and keeping other parameters fixed. To illustrate the effect of collisionality of the plasma, Fig. 5 shows the growth rate of the electrostatic ion cyclotron instability (Eq. (3)) as a function of altitude for profile B of Fig. 1,

assuming a pure  $O^+$ ,  $e^-$  plasma and taking  $k_{\perp}/k_{\parallel} = 0.06$ ,  $V_d/V_e = 0.3$ . The growth rate shown is based on  $b_{\perp} = k_{\perp}^2 \rho_i^2 / 2 = 1$  which gives maximum growth. Curve 1 represents the collisionless growth rate ( $\nu_e = 0 = \nu_i$ ). The decrease in growth rate is due to the decrease in  $\tau$  as one goes down in altitude. Curve 2 (where  $\nu_e \neq 0$ ,  $\nu_i = 0$ ), however, displays the strong destabilization in the 100 to 150 km region and mild destabilization around 300 km. Curve 3, (where  $\nu_e \neq 0$ ,  $\nu_i \neq 0$ ), on the other hand, shows the stabilizing influence of ion collisions. The damping influence of ion-ion collisions is phenomenologically represented by  $(\nu_{ii} b_{\perp}) / (1 + b_{\perp})$ , as discussed in the next paragraph. As a comparison we show in curve 4 the collisionless growth with only ion damping included ( $\nu_i \neq 0$ ,  $\nu_e = 0$ ). Curve 3 represents the growth rate for completely realistic ionospheric conditions for which parameters such as plasma density, electron and ion temperatures and neutral density vary with altitude. Curves 3 and 4 clearly establish the importance of the electron collisions, which overcome the ion damping in the region  $100 < z < 130$  and significantly enhance the growth rate in the region  $150 < z < 300$ .

Figure 6 displays the growth rate of the electrostatic ion cyclotron instability including both electron and ion collisions for the three electron density profiles in Fig. 1 and temperatures shown in Fig. 2 assuming an  $O^+$  ion plasma. Although not explicitly calculated in Eq. (3), the ion-ion collisional damping ( $\nu_{ii}$ ) is included in the calculation of the growth rates of Fig. 6 by modeling this damping with the expression  $-\nu_{ii} k_{\perp}^2 \rho_i^2 / (1 + k_{\perp}^2 \rho_i^2)$  (Y.C. Lee, private communication). This expression reduces to the appropriate viscous damping in both the magnetized ( $k_{\perp} \rho_i < 1$ ) and unmagnetized ( $k_{\perp} \rho_i \gg 1$ ) limits. Since we are concerned with bottomside characteristics of EIC waves ( $\nu_{ii} \leq \nu_{in}$ ), the growth rates will not be extremely sensitive to  $\nu_{ii}$  in any case. The ion-neutral collisions were treated by BGK model with  $\nu_{in} \propto n_0 T_i^{1/2}$ , where  $n_0$  is the neutral density. Finally, for Fig. 6 the following parameters  $k_{\perp}/k_{\parallel} = 0.06$ ,  $k_{\perp} \rho_i = \sqrt{2}$ , and  $V_d/V_e = 0.3$  are used. Curves A, B and C correspond to the profiles given in Fig. 1. It can be seen from curve A that the growth rate maximizes around 400 km and progressively decreases at lower altitudes due to increased damping by ion-neutral and ion-ion collisions and due to a decrease in the electron temperature ( $\tau$  decreases with decreasing altitude; see Fig. 2). Curve B, representing a typical

ionosphere has smaller growth rate than curve A above 250 km and slightly higher growth rate than curve A below 250 km. Although electron collisions lead to higher growth, the decrease in  $\tau$  has greater effect on the collisional instability than on the collisionless instability; hence, the decrease in the growth rate above 250 km. The increase in the growth rate at lower altitudes is mainly due to increased electron collisions. Curve C, representative of a disturbed ionosphere, has peak growth at  $\sim 250$  km in the F-region, the decrease in the growth rate at higher altitudes being mainly due to increased ion-ion collisional damping. Eventually the ion damping decreases at higher altitudes where the collisionless theory is valid above which altitude the growth rate increases due to increasing  $\tau$ .

Figure 7 gives the threshold drift velocities ( $V_d/V_e$ ) for the EIC instability for the three electron density profiles of Fig. 1 assuming an  $O^+$  ion plasma taking  $k_{\perp}/k_{\parallel} = 0.06$  and for maximally growing modes with  $k_{\perp} \rho_i = \sqrt{2}$ . For profile B, the electrostatic ion cyclotron instability could be destabilized in the bottomside ionosphere ( $\leq 300$  km) for current drift velocities on the order of a tenth of electron thermal velocities,  $V_d \leq 0.1 V_e$ . Curves A, B and C again are obtained using the density profiles given in Fig. 1. Comparing this figure with Fig. 6, we see that lower drift velocities are needed at larger growth rates. This figure also shows that the collisional EIC instability can also be excited in the E region, although it shows that it is easier to excite EIC in moderately collisional domain (Curve A) than under disturbed conditions (Curve C).

Figure 8 shows the growth rate of the EIC instability including both electron and ion collision for the three electron density profiles in Fig 1 assuming an  $NO^+$  ion plasma. The growth rates of the EIC instability for an  $NO^+$  plasma are similar to (though slightly lower than) the growth rate for the  $O^+$  plasma (Fig. 6). This is consistent with Eqs. (5), (12) and (17) which indicate that the  $\gamma/\Omega_i$  is not a strong function of ion mass. Note that the growth rate is normalized to respective gyro frequencies in each case.

Fig. 9 displays the threshold drift velocities ( $V_c/V_e$ ) for the EIC instability including both electron and ion collisions using the density profiles of Fig. 1 assuming  $NO^+$  ion plasma. Comparing Fig. 9 with Fig. 7 ( $O^+$  plasma) one notes a slight decrease in the threshold drift velocity as

one goes from  $O^+$  to  $NO^+$ . This is also consistent with previous studies (Drummond and Rosenbluth, 1962, Kindel and Kennel, 1971) which have shown that increasing the ion mass decreases the threshold current drift velocity at all  $T_e/T_i$  to excite the EIC instability. We have also calculated the growth rates and the critical drift velocities for the Hydrogen plasma. We find the growth rates of  $H^+$  EIC waves to be smaller and the critical drift velocities for excitation of  $H^+$  EIC waves to be much higher; for instance,  $V_c/V_e = 0.4$  for  $H^+$  EIC wave excitation for the typical parameters used for  $O^+$  calculations, as compared to  $V_c/V_e = 0.1$  for  $O^+$  excitation. These critical drift velocities correspond to extremely large currents and thus we can conclude that the  $H^+$  EIC waves are not likely to be excited in the bottomside ionosphere. For this reason we do not present the detailed results of  $H^+$  EIC wave calculations.

To further emphasize the heavy ion EIC excitation in the F region, we show the threshold currents in the altitude region 100 km to 600 km. We use the density profile ( $n_e$ ) from Curve A of Fig. 1,  $T_e$  from Fig. 2 and ( $V_c/V_e$ ) from Figs. 7 and 9 to calculate the threshold current  $J = n_e e V_c$ . Figure 10 shows the threshold currents required to excite  $O^+$  EIC and  $NO^+$  EIC in  $O^+$  and  $NO^+$  plasmas, respectively for  $k_{\perp} \rho_i = \sqrt{2}$  and  $k_{\parallel}/k_{\perp} = 0.06$ . It is clear from Fig. 10 that  $NO^+$  EIC has lower thresholds than  $O^+$  EIC and the altitude region between 150 km and 200 km and the region above 400 km have lower thresholds. The currents shown near 100 km may not be accurate because the theory may not be valid in this region due to demagnetization of the ions ( $v_{in}/\Omega_i \sim 1$ ). The critical currents corresponding to curves B of Figs. 1, 7 and 9 (not shown here) are of the order  $200 \mu A/m^2 - 1000 \mu A/m^2$ . Thus, for typical ionospheres such as those given by curve B, one requires large currents to support  $O^+$  or  $NO^+$  EIC. Although our calculations are applicable to plasma with single ion species, based on the results presented in Figs. 7, 9, and 10 we can draw qualitative conclusions regarding a multispecies plasma, namely that when  $H^+$ ,  $O^+$ ,  $O_2^+$  and  $NO^+$  species are present, EIC waves of heavier species are more susceptible to destabilization by parallel currents. Thus we conclude that  $NO^+$  or  $O_2^+$  EIC instability can be excited more easily in the bottomside F region than the  $H^+$  or  $O^+$  EIC instability. This is consistent with the photometric observations of Martelli et al. [1971].

### 3. Nonlinear Saturated Amplitudes

In the previous section we showed that the collisional electrostatic ion cyclotron instability could be important in the bottomside high latitude ionosphere. In this section we discuss a possible nonlinear mechanism that might saturate these modes. In the literature several nonlinear saturation mechanisms for the electrostatic ion cyclotron instability have been studied. Davidson (1972) has discussed large amplitude trapping effects which become important when  $\omega_t \tau_c \gg 1$  where  $\omega_t = k_{\parallel} (e\phi/m_e)^{1/2}$  is the electron trapping frequency and  $\tau_c = k_{\parallel} \Delta v$  is the wave correlation time,  $\phi$  is the wavepotential,  $k$  is the wavevector, and  $\Delta v$  is the spread in wave phase velocities parallel to the magnetic field. Collisional effects will prevent strong electron trapping. Another mechanism is ion resonance broadening [Dum and Dupree, 1970]. In this work we extend Dum and Dupree's theory to the case of the collisional EIC instability. Physically, the effect of the turbulence generated by the instability may be interpreted as an enhanced ion viscosity. In this section we shall present only estimates of the saturation amplitudes for typical ionospheric parameters and not a comprehensive full F-region study.

The nonlinear dispersion relation for the electrostatic ion-cyclotron modes, including the effects of resonance broadening, may be obtained by substituting  $\bar{\omega} \equiv \omega + i\Delta\omega^w$  in lieu of  $\omega$  in the ion contribution to Eq. (3) [Dum and Dupree, 1970]. Here  $\Delta\omega^w$  is the modification introduced by the effect of a spectrum of finite amplitude modes on the particle orbits (resonance broadening effect). Thus,

$$1 + \epsilon_e^l(k, \omega) + \epsilon_i^{nl}(k, \omega + i\Delta\omega^w) = 0 \quad (23)$$

is the nonlinear dispersion relation for the EIC modes, where  $\epsilon_j^l$  is the linear dielectric constant and  $\epsilon_j^{nl}$  is the nonlinear dielectric constant. We note that Dum and Dupree [1970] have shown the effect of resonance broadening is important only for ions in the EIC wave case. Hence the contribution coming from the resonance broadening effect on electrons has been ignored in the expression (23). One may obtain an estimate for the nonlinear saturated amplitudes of EIC modes from (23) by setting the nonlinear growth rate  $\gamma^{nl}$

$$\gamma^{nl} = \gamma_k^l - \Delta\omega^w = 0 \quad (24)$$

where  $\gamma_k^l$  is the linear growth rate of the mode with wavenumber  $k$ . For the EIC instability case,  $\Delta\omega^w$  may be approximated as [Dum and Dupree, 1970],

$$\Delta\omega^w = (\omega - \Omega_i) \left[ \left( \frac{n_1}{n_1^0} \right)^2 - 1 \right]^{1/2} \quad (25)$$

Here  $n_1$  is the saturated nonlinear amplitude of the wave, and,  $n_1^0$  is the threshold level of the nonlinear amplitude at which the resonance broadening effects assume importance. The expression for  $n_1^0$  is

$$\begin{aligned} \frac{n_1^0}{n} &= \left( \frac{T_i}{2T_e} \right) \left( \frac{\Omega_i}{k_{\perp} v_i} \right)^2 \frac{(\omega_k - \Omega_i)}{\Omega_i [F_1(\mu_i)]^{1/2}} \\ &= \left( \frac{T_i}{2T_e} \right) \frac{1}{\mu_i (F_1)^{1/2}} \left( \frac{\omega - \Omega_i}{\Omega_i} \right) \end{aligned} \quad (26)$$

where 
$$F_1(x) = \begin{cases} \frac{1}{4} \left[ 1 - \frac{1}{4} \left( \frac{x}{2} \right)^4 + \frac{1}{9} \left( \frac{x}{2} \right)^6 + \dots \right], & \text{for } x \leq 2 \\ \frac{1}{\pi x}, & x \geq 3 \end{cases}$$

It may be noted that the broadening of resonances above corresponds to an enhancement in the group of ions that can exchange energy with the wave via resonance interaction. Stabilization of the mode results when the resonance is broadened to an extent such that the bulk of the ion distribution interacts with the wave and absorbs energy from it, thereby, leading to a steady finite amplitude nonlinear state. We now use expressions (24)-(25), to compute the nonlinear saturated amplitudes for the collisional EIC modes. From (24) and (25), one has

$$(\omega - \Omega_i) \left[ \left( \frac{n_1}{n_1^0} \right)^2 - 1 \right]^{1/2} = \gamma_k^l \quad (27)$$

which leads to

$$\left( \frac{n_1}{n} \right)^2 = \left( \frac{n_1^0}{n} \right)^2 \left[ 1 + \frac{(\gamma_k^l)^2}{(\omega - \Omega_i)^2} \right] \quad (28)$$

or

$$\left(\frac{n_1}{n}\right)^2 = \frac{\left(\frac{T_i}{T_e}\right)^2 \left(\frac{\Omega_i}{k v_i}\right)^4 \left(\frac{\omega_r - \Omega_i}{\Omega_i}\right)^2}{F_1\left(\frac{1}{\Omega_i}\right)} \left[ 1 + \frac{\left\{ \frac{T_e}{T_i} \Omega_i \Gamma_1 \frac{v_e}{k^2 v_e^2} (k v_d - \omega_r) - k_{\perp}^2 \rho_{ii}^2 v_{ii} - v_{in} \right\}^2}{(\omega_r - \Omega_i)^2} \right] \quad (29)$$

using (17) and including  $v_{ii}$  collisions.

For the case,  $T_e = T_i$ , one has

$$(\omega - \Omega_i) = \Omega_i \Gamma_1$$

which leads to

$$\left(\frac{n_1}{n}\right)^2 = \frac{\left(\frac{\Omega_i}{k v_i}\right)^4 \Gamma_1^2}{F_1\left(\frac{1}{\Omega_i}\right)} \left[ 1 + \left\{ \frac{v_e}{k^2 v_e^2} (k v_d - \omega_r) - \frac{k_{\perp}^2 \rho_{ii}^2 v_{ii} - v_{in}}{\Omega_i} \right\}^2 \right] \quad (30)$$

The expression (30) gives the nonlinear saturated amplitudes of density fluctuations associated with the collisional ion-cyclotron modes due to resonance broadening effects in the presence of both electron ( $v_e$ ), ion-ion ( $v_{ii}$ ) and ion-neutral ( $v_{in}$ ) collisions applicable to bottomside ionospheric altitudes. A comparison with the collisionless case, discussed by Dum and Dupree [1970], shows that the saturated amplitudes can be higher in the collisional case, by an increment of approximately  $\sim \frac{1}{2}[(v_d/v_e)(1/k \lambda_e)]^2$ . We note that, in the above comparison, it is implied that  $\gamma_{kc}/(\omega_k - \Omega_i) \ll 1$ , where  $\gamma_{kc}$  is the collisionless growth rate.

#### 4. Summary and Discussion

In this study we have presented a comprehensive treatment of the theory of the electrostatic ion cyclotron instability in the collisional bottomside ionosphere. We have derived the linear dispersion relations for the ion cyclotron instability including both electron and ion collisions and solved analytically the dispersion relation in three limits: collisionless, weakly collisional, and collisional. In addition, we have solved the linear dispersion relation exactly using numerical methods using

parameters typical of the high latitude bottomside ionosphere. We note that the linear growth rates in the bottomside collisional regime can be of the same order as the corresponding topside collisionless growth rates. We have considered three cases corresponding to three different ionospheric conditions. The normal ionosphere is bracketed by two others with minimum density around  $10^4 \text{ cm}^{-3}$  at the lower end and maximum peak density of  $10^6 \text{ cm}^{-3}$  at the high end. The former represents a weakly collisional case ( $\nu_e/\Omega_e < 10^{-4}$ ) and this can be considered as an extension of the previous collisionless EIC instability theories, the latter represents disturbed conditions, yielding high electron collisions and ion collisions. We have also considered pure  $O^+$  and pure  $NO^+$  plasmas and solved the dispersion relation for single species in both cases. We arrive at the following conclusions based on the linear calculation.

- a. Given the realistic ionospheric parameters, we find that the theory of collisionless EIC instability (Kindel and Kennel, 1971) can not be extended to the bottomside F region ( $z < 400 \text{ km}$ ). Since, the critical drift velocities and growth rates are sensitive to  $n_e$  and  $T_e/T_i$ , a theory of collisional EIC using self-consistent collision frequencies and  $T_e/T_i$  should be used for accurate prediction of EIC excitation.
- b. Electron collisions destabilize the EIC wave which results in higher growth rates. However, the ion-ion collisions damp the modes, the damping being equal to  $\nu_{ii}$  in  $k_{\perp} \rho_i \gg 1$  limit and  $\nu_{ii} k_{\perp}^2 \rho_i^2 / 2$  in the  $k_{\perp} \rho_i \ll 1$  limit. The EIC instability growth rate maximizes for  $k_{\perp} \rho_i \geq 1$ .
- c. For realistic profiles of the ionosphere, the collisional EIC wave growth rates are reduced by ion-neutral collisions in the bottomside F region and by ion-ion collisions above 300km, as expected.
- d. For profiles given in Fig. 1, the collisionless theory (ion collisions dominate electron collisions) prevails for curve A and collisional theory (electron collisions are stronger and dominate ion collisions) prevails for curve C.



- e. The growth rate maximizes in the weakly collisional (curve A, Fig. 1) regime at an altitude of 400 km and in the strongly collisional (curve C, Fig. 1) regime at an altitude of 250 km. In the collisional domain, (curve C, Fig 6) the growth rate has minimum at an altitude of 300 km and achieves a further lower value at E region altitudes (150 km or less).
- f. The critical drift velocity required to excite the EIC waves is sensitive to the electron densities and thus are quite different in the collisionless and collisional domains. It is smaller at higher altitudes,  $z < 400$  km, and larger at lower altitudes,  $z < 200$  km.
- g. For realistic ionospheric profiles, the growth rate is weakly dependent on the mass ratio ( $m_e/m_i$ ). However, we find that the critical drift velocity is much smaller for EIC waves corresponding to gyrofrequencies of heavier ions than the critical drift corresponding to lighter ion ( $H^+$ ) EIC wave excitation. Our single species calculation shows that  $NO^+$  or  $O_2^+$  EIC instability are much easier to excite than  $O^+$  or  $H^+$  EIC instability. Thus, in a multi-component plasma EIC waves at  $NO^+$  will be first excited before, for example,  $O^+$  EIC waves and in the bottomside ionosphere EIC instability at  $H^+$  gyrofrequency is unlikely to be excited.

In addition, we have discussed a nonlinear saturation mechanism for the electrostatic ion cyclotron instability in the collisional regime based upon Dupree's ion resonance broadening theory. Dupree's resonance broadening theory is valid only for a broad spectrum of waves which are assumed isotropic and incoherent, i.e., the wave coherence time (spectral width) is much shorter than an ion cyclotron period. For a narrow (coherent) wave spectrum, resonance broadening theory must be replaced by an analysis which considers exact ion dynamics in a coherent wave [Davidson, 1972; Aamodt, 1970]. Recent nonlinear numerical simulations [Pritchett et al., 1981; Okuda and Ashour-Abdalla, 1981] of the collisionless ion cyclotron instability indicate a large amplitude coherent wave spectrum in the nonlinear regime. However these simulations also show several modes excited in the saturation phase of the ion cyclotron

instability. To our knowledge, there have been no nonlinear simulations of the collisional current-driven ion cyclotron instability. We shall now discuss some particular examples of the auroral ionospheric application of the collisional EIC instability.

In a recent study using sounding rockets, Yau et al. (1983) have recorded  $O^+$  waves and strong perpendicular ion acceleration (ion conics) events at low altitudes (400-600 km) in the high latitude ionosphere during the expansive phase of an auroral substorm. Large relative density fluctuations ( $\leq 10\%$ ) were also recorded near the ion conic acceleration regions. One major candidate for conic formation is EIC wave heating [Ungstrup et al., 1979; Okuda and Ashour-Abdalla, 1981]. Considering typical high latitude parameters, i.e.,  $T_e = T_i = 0.1$  eV, electron density corresponding to curve A of Fig. 1, ( $n_e \sim 3 \times 10^4$ ,  $v_e/\Omega_e \sim 2 \times 10^{-5}$ ,  $v_i/\Omega_i \sim 7 \times 10^{-3}$ ) the growth rate of  $O^+$  EIC waves, with  $\lambda_{\perp} \sim 11$  m ( $k_{\perp} \rho_i \sim 1.4$ ,  $\rho_i \sim 2.56$  m for  $O^+$  ions) and  $\lambda_{\parallel} \sim 200$  m, is  $0.07 \Omega_i$  or  $21 \text{ sec}^{-1}$ , taking  $\Omega_i$  for  $O^+$  in a 0.5 Gauss magnetic field as 300 Hz (Fig. 6, curve A). The corresponding growth rate for  $NO^+$  EIC waves ( $\lambda_{\perp} \sim 15$  m) is  $0.08 \Omega_i$  or  $12 \text{ sec}^{-1}$ , taking  $\Omega_i$  to be 150 Hz. The critical drift velocities can be read off Fig. 7 for  $O^+$  ions. For the above parameters the critical drift velocity at an altitude of 300 km, for example, is  $0.09 V_e$  (Curve A, quiet conditions) which corresponds to  $53 \mu\text{A}/\text{m}^2$  for  $n_e \sim 3 \times 10^{10}/\text{m}^3$ . For  $NO^+$  ions, under the same conditions, the critical drift velocity is  $\sim 0.06 V_e$  (Fig. 9) which corresponds to  $40 \mu\text{A}/\text{m}^2$ . For other profiles, Curves B (normal conditions) and C (disturbed conditions) of Fig 1 critical drift velocities are higher and require currents  $> 100 \mu\text{A}/\text{m}^2$  and  $\sim 1000 \mu\text{A}/\text{m}^2$ , respectively. In view of these results we find that the ionospheric conditions corresponding to curve A of Fig. 1 are most conducive to EIC excitation at  $NO^+$  and  $O_2^+$  gyrofrequencies. From equation (30), the saturated amplitude for typical parameters i.e.,  $T_e = T_i = 0.1$  eV,  $\Omega_i = 3 \times 10^2 \text{ sec}^{-1}$ ,  $v_e = 10^{-4} \text{ sec}^{-1}$ ,  $v_{in}/\Omega_i = 10^{-3}$ ,  $v_{ii}/\Omega_i \sim 10^{-2}$  is found to be approximately  $n_1/n_0 = 0.24$  according to ion resonance-broadening theory for  $k_{\perp} \rho_i = 1.2$ ,  $k_{\parallel}/k_{\perp} = 0.1$ , and  $v_d \geq 2 \times 10^6 \text{ cm/sec}$ . We note that the saturation amplitude  $n_1/n_0$  of EIC waves in the collisionless regime, using Eq. (30), is slightly smaller ( $n_1/n_0 = .22$ ) than the collisional case.

Compelling evidence of the presence of energetic heavy ionospheric ions at high altitudes ( $> 1000$  km) (Hultqvist, 1983; Klumpar et al., 1984; Yau et al., 1984) leads one to suggest that the bottomside ionosphere, which is a source of heavy ions, is indeed acting as an accelerating region for these heavy ions (Hultqvist, 1983). Furthermore, energetic heavy ions,  $\text{NO}^+$  and  $\text{O}_2^+$ , have been observed at outer magnetospheric altitudes on days of high geomagnetic activity (Klecker et al., 1985; Craven et al., 1985). High geomagnetic activity at higher altitudes is usually indicative of a disturbed ionosphere, which could sustain large ionospheric currents that drive collisional EIC waves in the bottomside ionosphere unstable. Thus, we conjecture that the ion cyclotron instability at the ion (heavy) cyclotron frequency, driven unstable by parallel field-aligned currents may selectively accelerate the  $\text{NO}^+$ ,  $\text{O}_2^+$  and  $\text{O}^+$  ions in the transverse direction at low altitudes and these transversely accelerated ions form the heavy ion conics at the higher altitudes.

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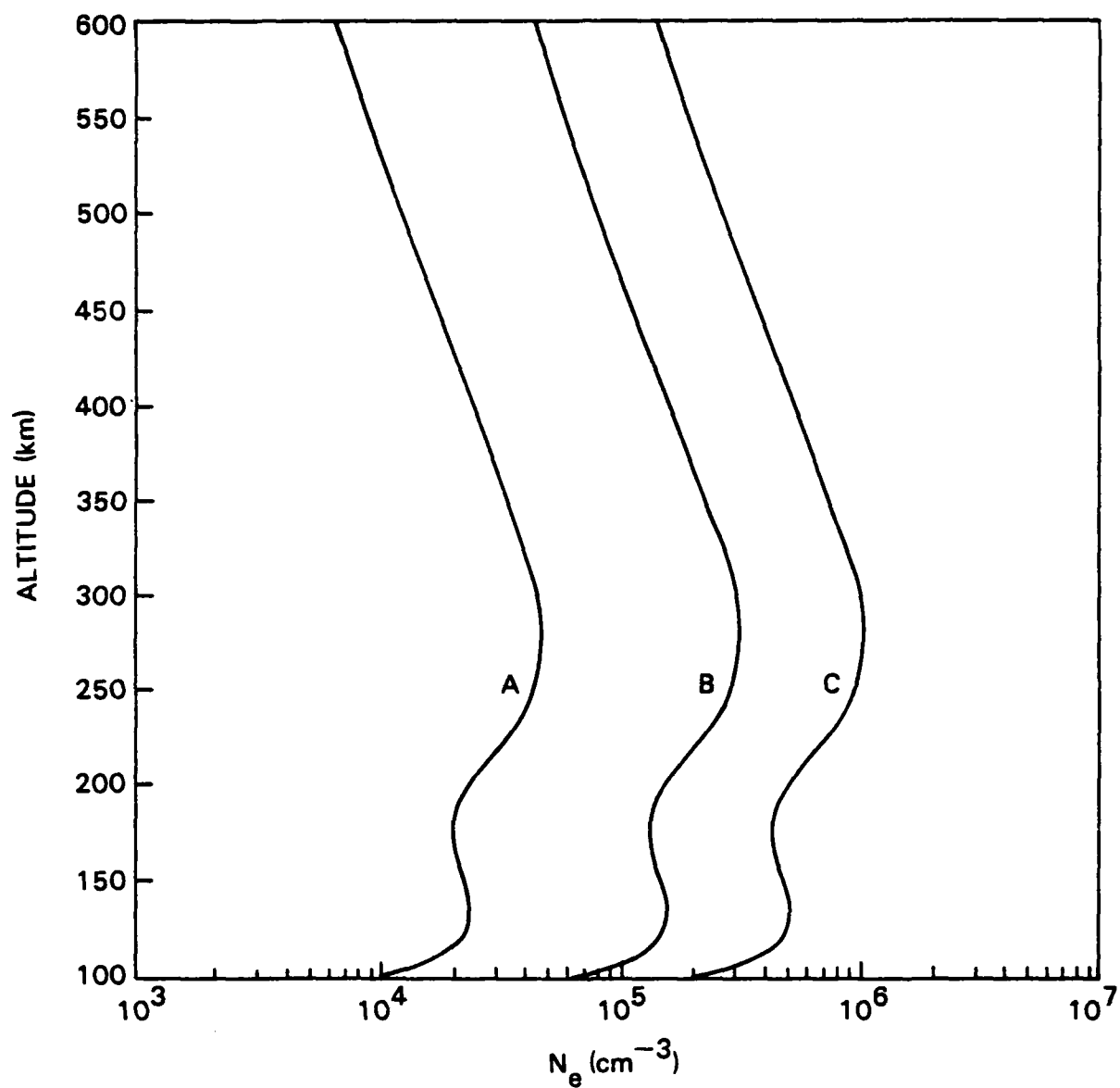


Fig. 1 Typical ionospheric electron density profiles based on Sondrestrom incoherent scatter radar data. Curve A represents a quiet condition, curve B an intermediate electron density, and curve C a disturbed condition.

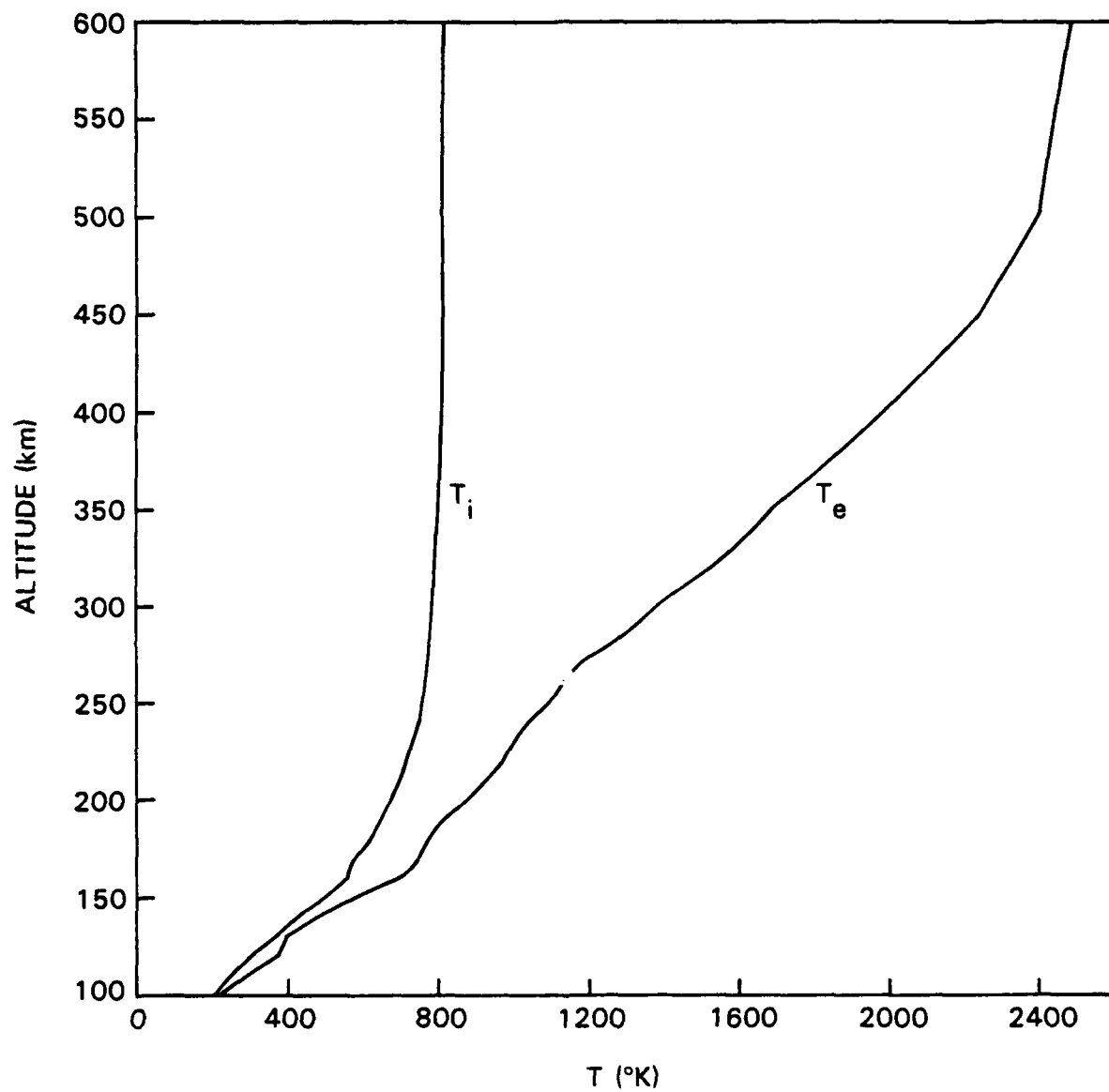


Fig. 2 Typical temperature profiles for  $T_e$  and  $T_i$  vs. altitude, based on Sondrestrom data.

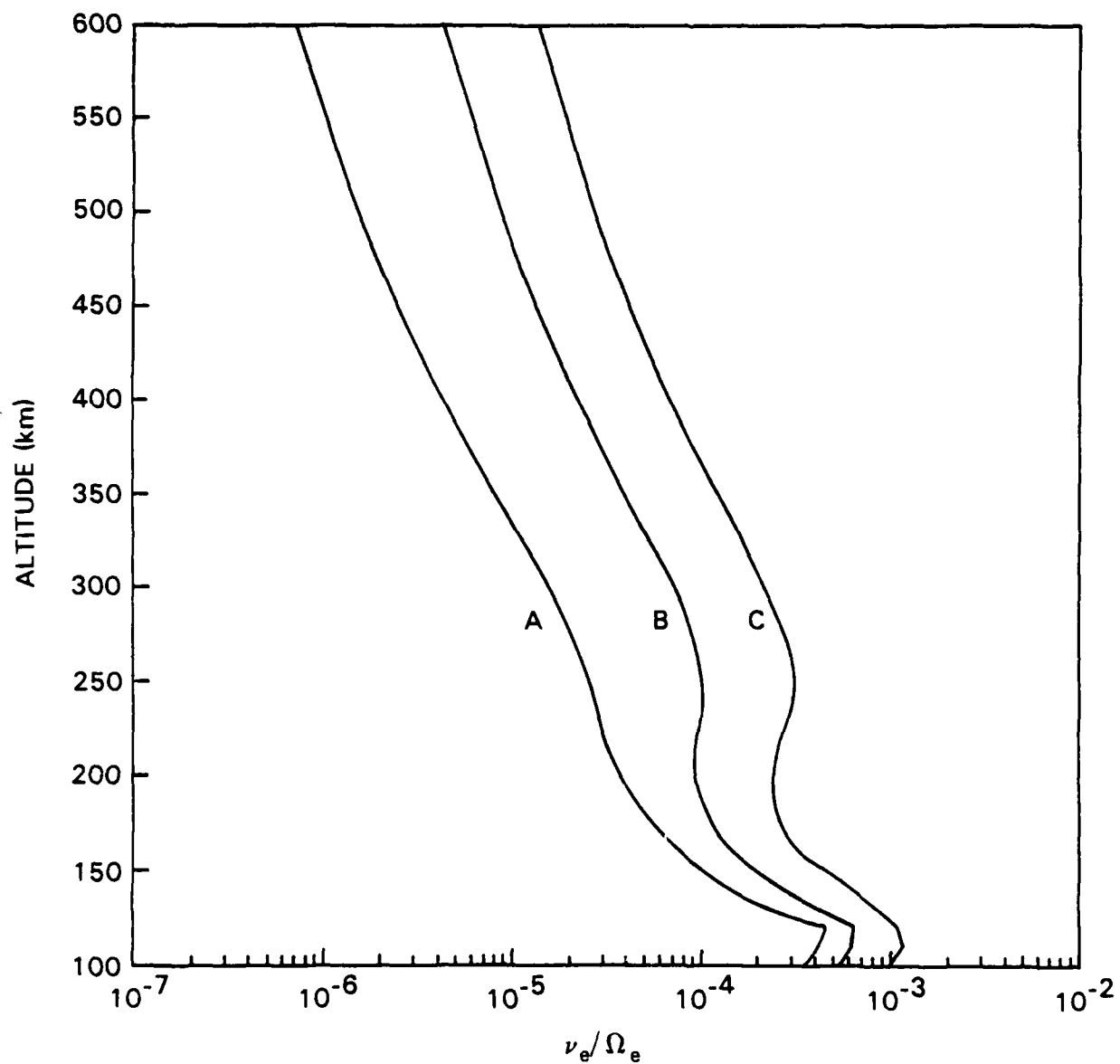


Fig. 3 Total electron collision frequencies( $\nu_e/\Omega_e$ ) where ( $\nu_e = \nu_{en} + \nu_{ei}$ ) vs. altitude.

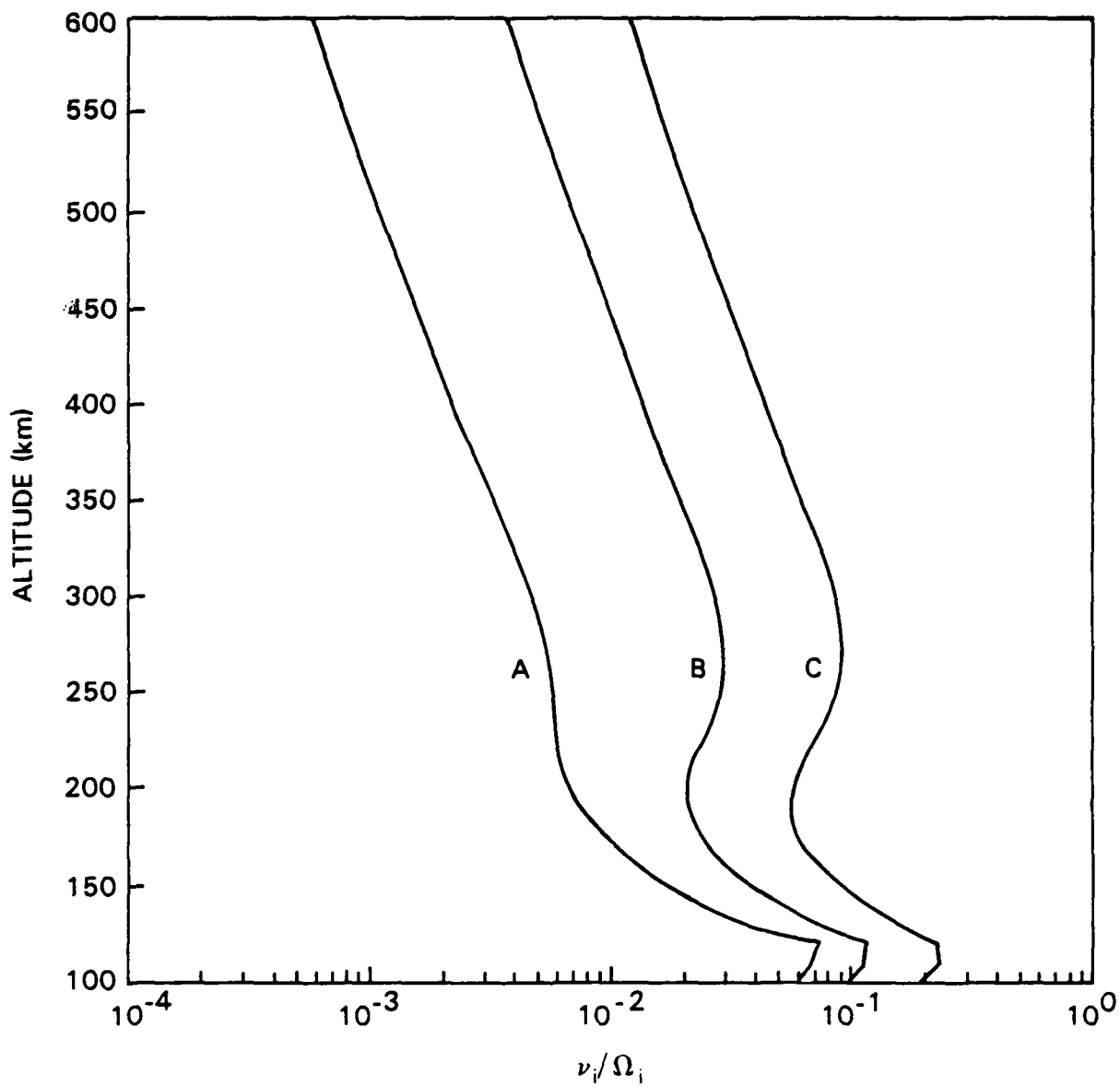


Fig. 4 Total ion collision frequencies ( $\nu_i = \nu_{in} + \nu_{ii}$ ) with neutrals ( $\nu_{in}$ ) and ions ( $\nu_{ii}$ ) vs. altitude.



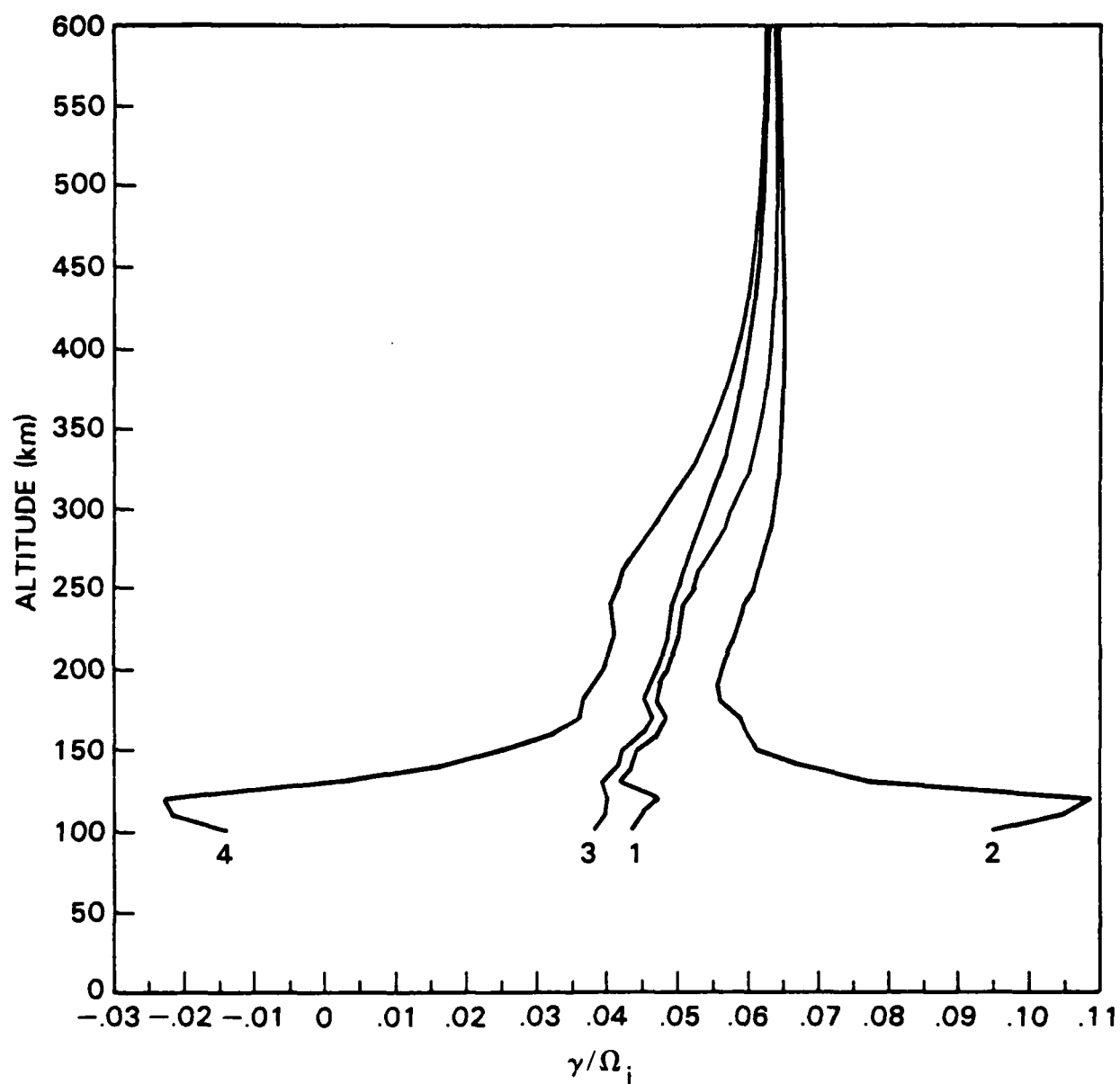


Fig. 5 Growth rate  $\gamma/\Omega_i$  of electrostatic ion cyclotron instability vs. altitude for  $O^+$  ion plasma using curve B of Fig. 1 and taking  $\tau$  as varying with altitude and  $v_e = v_i = 0$  (curve 1);  $v_e = v_e(z)$ ,  $v_i = 0$  (curve 2);  $v_e = v_e(z)$ ,  $v_i = v_i(z)$  (curve 3); and  $v_e = 0$ ,  $v_i = v_i(z)$  (curve 4). Here  $k_{\perp}/k_{\parallel} = 0.06$ ,  $k_{\perp} \rho_i = \sqrt{2}$  and  $V_d/V_e = 0.3$ .

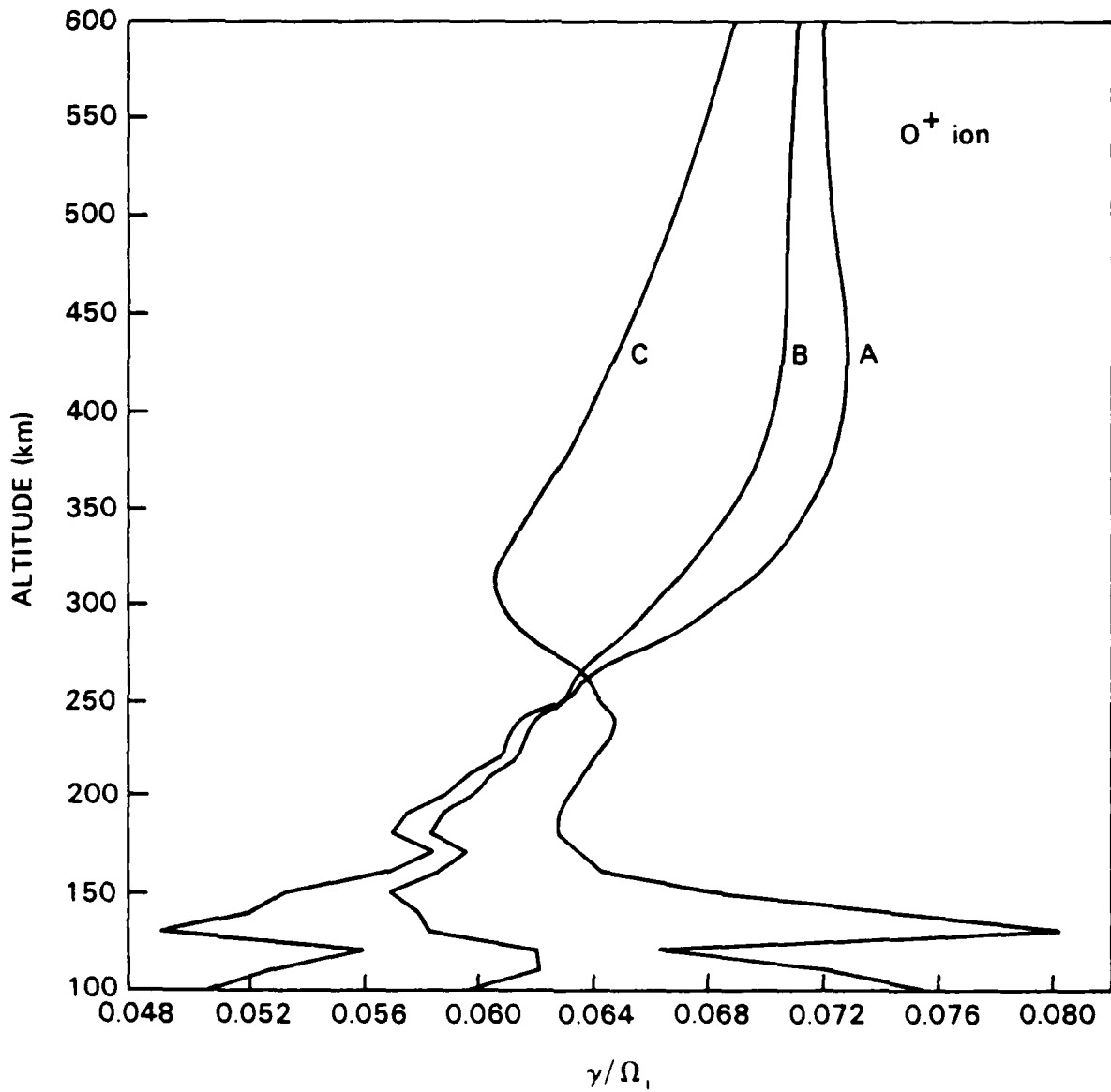


Fig. 6 Growth rate  $\gamma/\Omega_i$  of electrostatic ion cyclotron instability vs. altitude for  $O^+$  ion plasma using curves A-C of Fig. 1 with fixed parameters  $k_{\perp}/k_{\parallel} = 0.06$ ,  $k_{\perp}\rho_i = \sqrt{2}$  and  $V_d/V_e = 0.3$ .

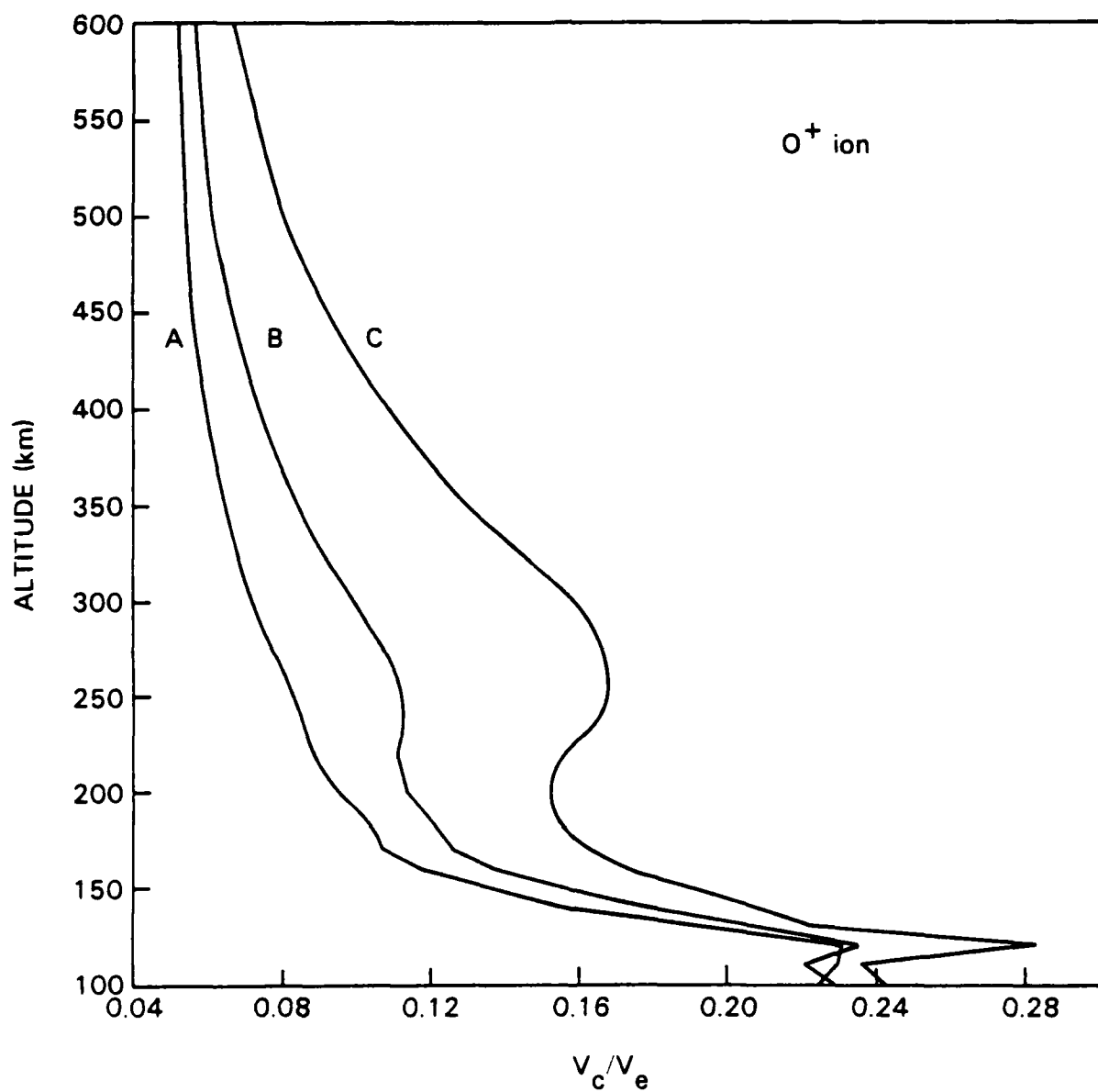


Fig. 7 Critical current drift velocity ( $V_c/V_e$ ) for excitation of electrostatic ion cyclotron instability vs. altitude for curves A-C of Fig. 1 for  $O^+$  ion plasma and  $k_{\parallel}/k_{\perp} = 0.06$ ,  $k_{\perp}\rho_i = \sqrt{2}$ .

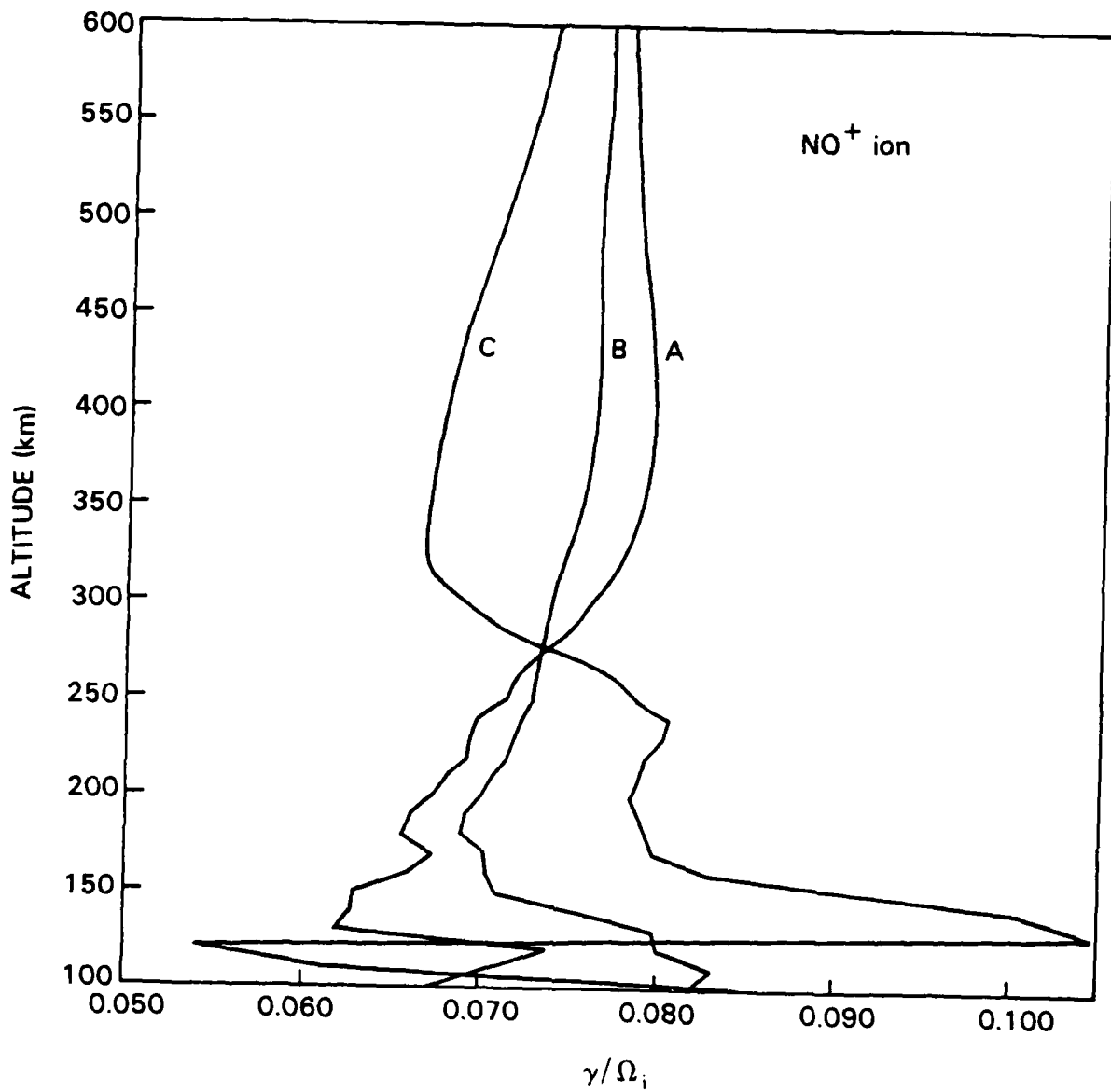


Fig. 8 Growth rate  $\gamma/\Omega_i$  of electrostatic ion cyclotron instability vs. altitude for  $\text{NO}^+$  ion plasma using curves A-C of Fig. 1 with fixed parameters  $k_{\perp}/k_{\parallel} = 0.06$ ,  $k_{\perp}\rho_i = \sqrt{2}$  and  $V_d/V_e = 0.3$ .

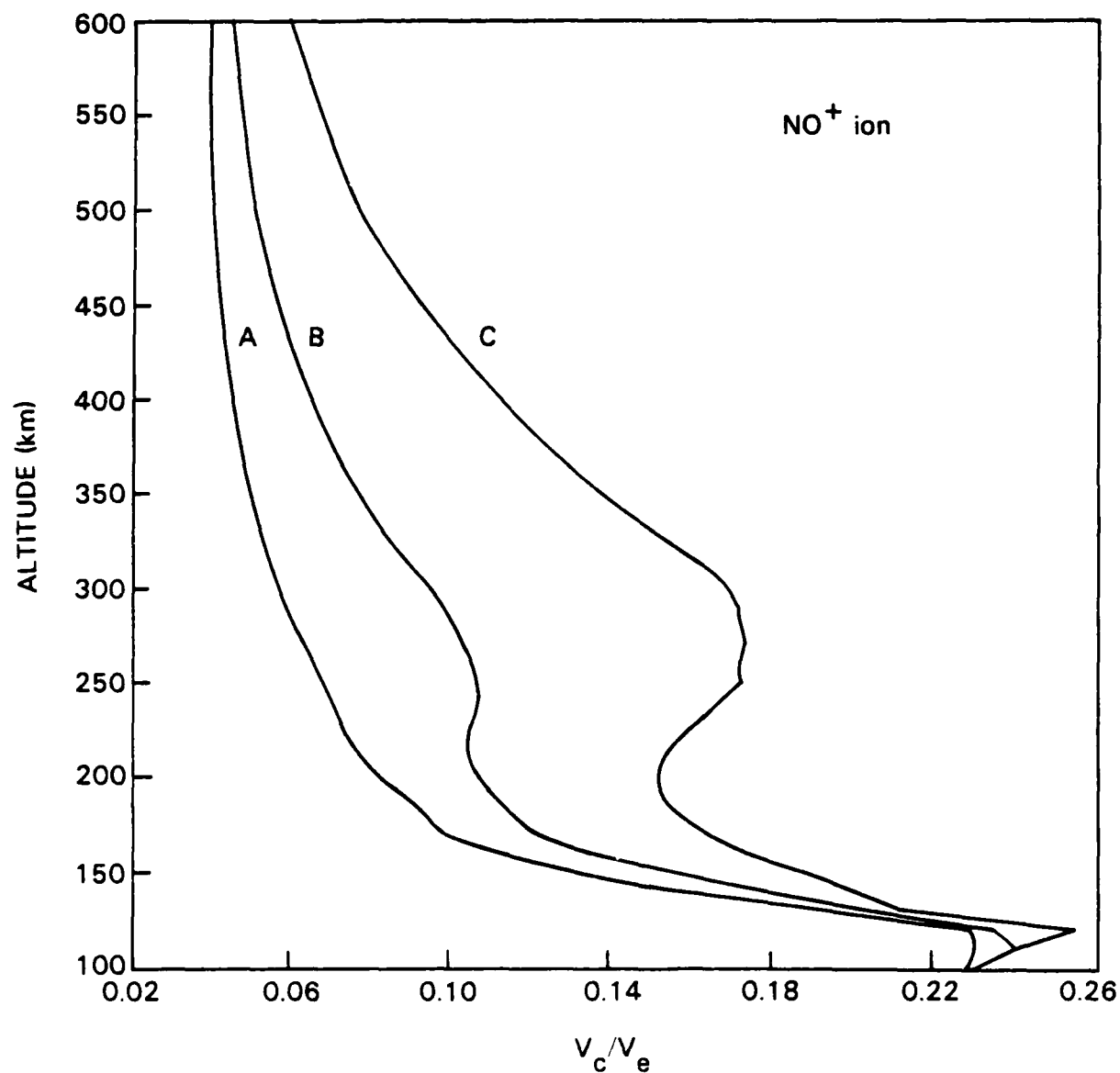


Fig. 9 Critical current drift velocity ( $V_c/V_e$ ) for excitation of electrostatic ion cyclotron instability vs. altitude for curves A-C of Fig. 1 for NO<sup>+</sup> ion plasma and  $k_{\parallel}/k_{\perp} = 0.06$ ,  $k_{\perp}\rho_i = \sqrt{2}$ .

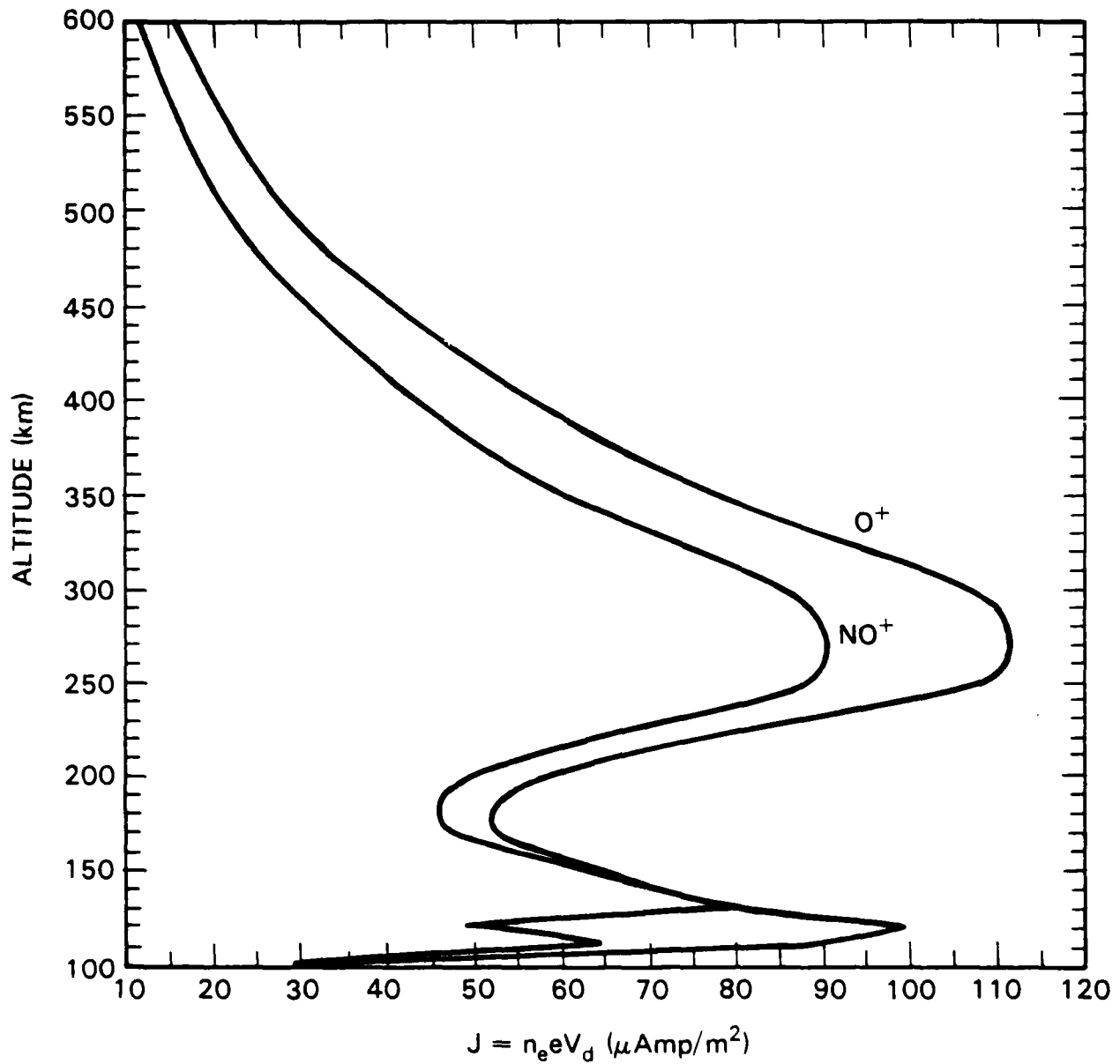


Fig. 10 Threshold currents in  $\mu\text{A}/\text{m}^2$  required to excite  $\text{O}^+$  and  $\text{NO}^+$  EIC waves in  $\text{O}^+$  and  $\text{NO}^+$  plasmas, respectively. The critical currents are calculated for  $J = n_e e V_d$  using  $V_c/V_e$  from curves A of Figs. 7 and 9,  $n_e$  from curve A of Fig. 1 and  $T_e$  from Fig. 2. The parameters used are  $k\rho_1 = \sqrt{2}$  and  $k_{\parallel}/k_{\perp} = 0.06$ .

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